

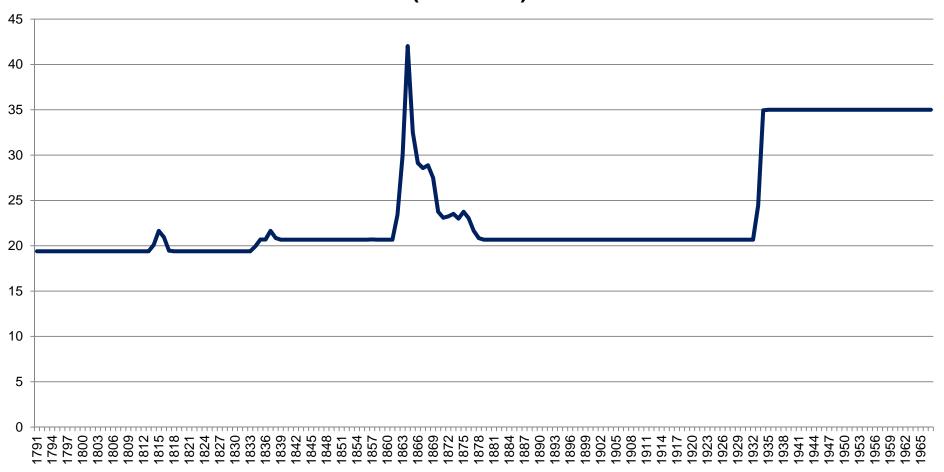
Based on "Is Gold Overpriced?" Lingjie Ma and George Patterson Journal of Investing Spring 2013, Volume 22, Number 1

Gold -- A truly unique asset

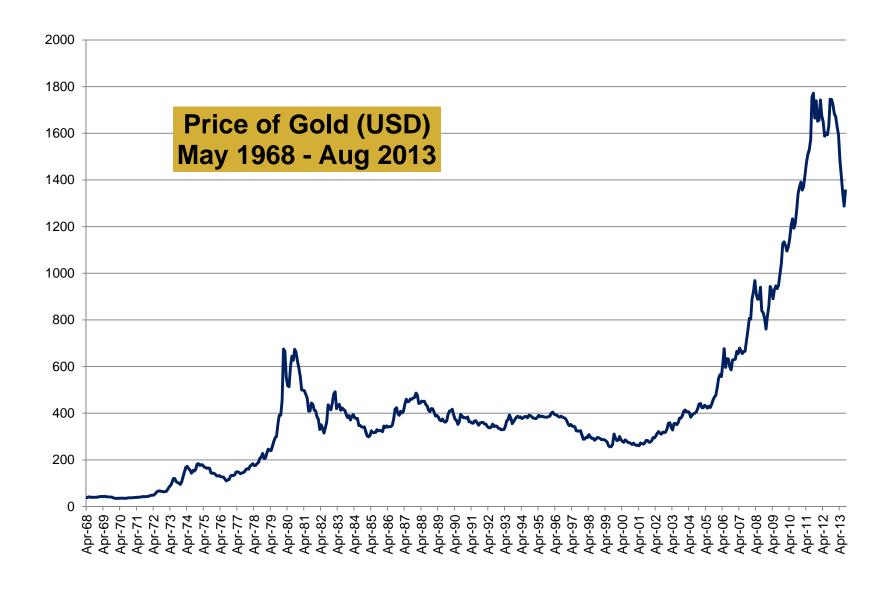
- Unlike other assets, gold truly is scarce.
- Few industrial uses even today.
- Unique supply & demand features due to hoarding & disposal.
- Most of the gold ever mined still exists in use today, in the form of jewelry or bullion. Jewelry can re-enter the market at the right price.
- Getting more difficult to find.
- Significant lead time to bring on new supply.
- Historical cornerstone of Central Bank reserves.
- Historical precedents in the manner in which it has been "used".

We have gone from this...

Gold Price (USD / Oz) 1791 - 1967



To This...



Understanding the price of this asset

- Identify key drivers that capture the:
 - Macroeconomy
 - Monetary System
 - Financial markets
 - Other significant commodities primarily Oil.
- Supply & Demand
- Identify proxies for these variables that:
 - Have the longest and most consistent time series.
 - Accurately capture the drivers that we consider.
- While economic data is reported with a lag, we can reverse the relationship to identify what the price of gold tells us about the current and future economy.

Key Findings

- Gold is not over priced in the recent period, except for a few months at the end of 2011.
- Very different result than if you apply a traditional ordinary least squares technique (OLS), which implies that gold has been over priced for some time.
- Strongest explanatory variables include:
 - Oil
 - US Dollar Index
 - Unemployment
- Evidence of gold being an inflation hedge is limited to a very specific time period.

Easy reserves have been mined...



We have gone from this approach

To this approach...



OLS vs. Quantile Regression

- Least squares captures how the mean of y changes with x
- Sometimes a single mean response is not enough for various reasons:
 - Some investigations are interested in extreme values, such as how a treatment impacts the extremes of a distribution (ex: Low birth weight risk factors, Educational analysis).
 - The distribution of independent variable may be asymmetric about the mean.
 - Heteroscedasticity.
- Benefits of Quantile Regression
 - Developed as an complement to least squares regression with the explicit purpose of estimating rates of change in all parts of the distribution.
 - We can still connect with the results of more traditional regression approaches.
 - Permit one to also investigate the confidence interval in addition to the response.
 - More general than least squares non parametric.

Ordinary Least Squares vs. Quantile Regression

OLS:

$$y_i = \beta \ x_i + \ \varepsilon_i$$

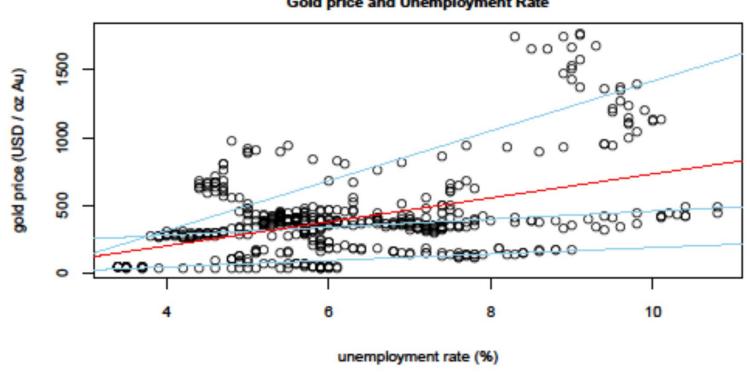
$$\hat{\beta} = \operatorname{argmin} \sum_{i=1}^{n} (y_i - x_i \beta)^2$$

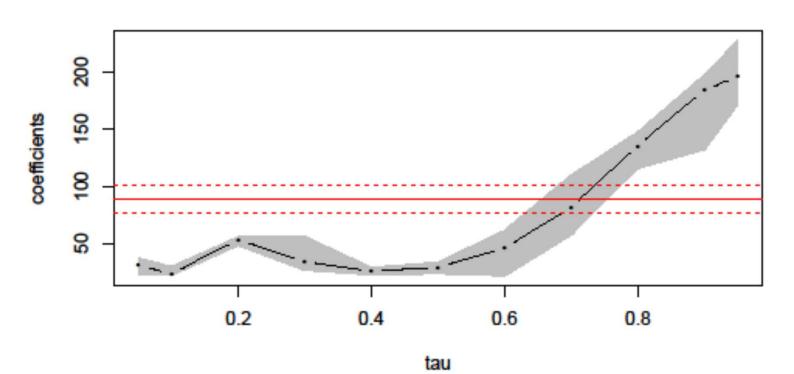
QR:

$$y(\tau) = x \beta(\tau)$$
 $0 < \tau < 1$

$$\hat{\beta}(\tau) = argmin\left[\tau \sum_{y \ge \beta x} (y_i - \beta x_i) + (\tau - 1) \sum_{y < \beta x} (y_i - \beta x_i)\right]$$

Gold price and Unemployment Rate





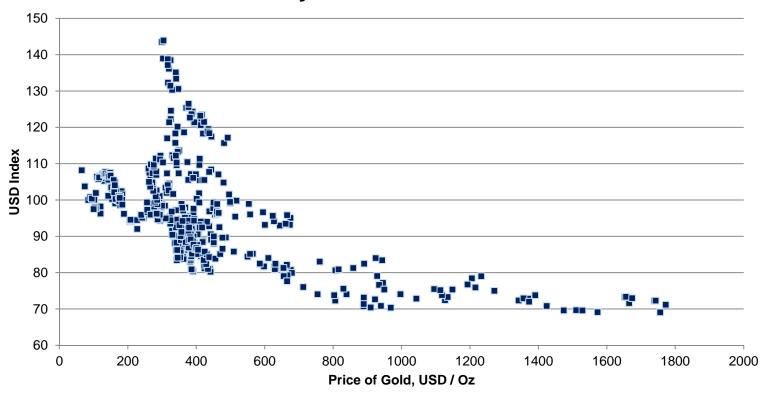
Key drivers / correlations

Pooled correlations between the price of gold & key variables in this study April 1968 – March 2012

	Correlation with the			
Variable	Price of Gold			
Oil	0.876			
Unemployment	0.462			
DJIA	-0.021			
TBILL	-0.196			
Inflation	-0.235			
GDP	-0.364			
USD Index	-0.587			

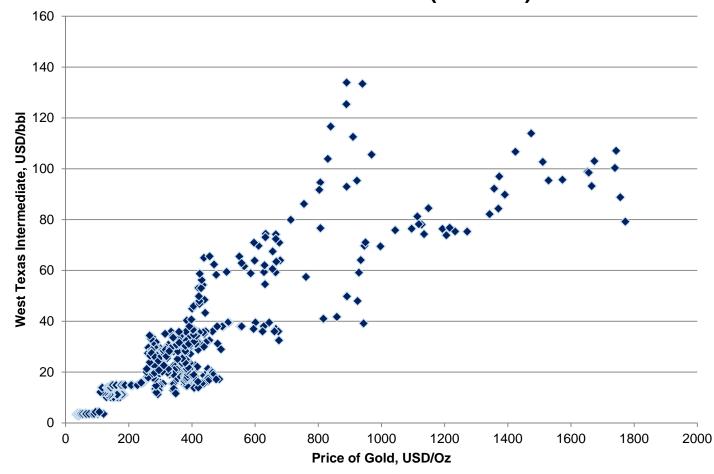
Hedge against a weak dollar? Yes!

US Dollar Index vs. Price of Gold May 1968 - Dec 2012



Correlated with oil? Yes!

West Texas Intermediate (USD/bbl) vs. Price of Gold (USD/Oz)



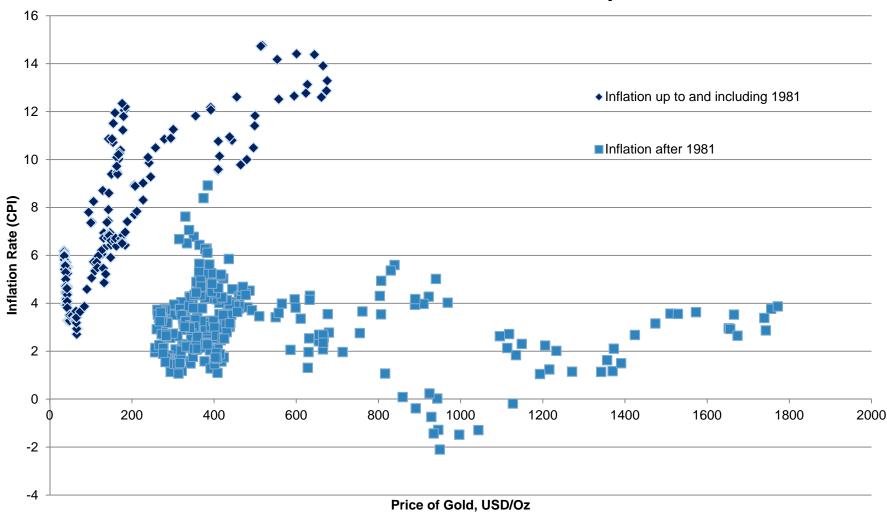
Inflation – The need for structural breaks

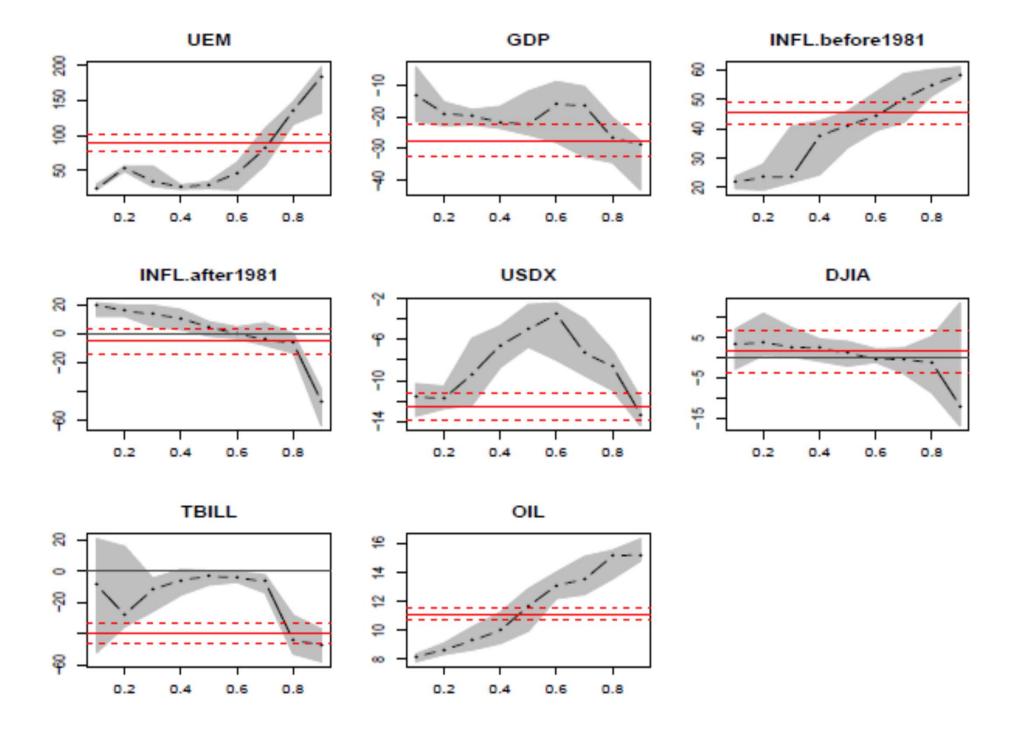
Real Inflation Rate (CPI) over Time

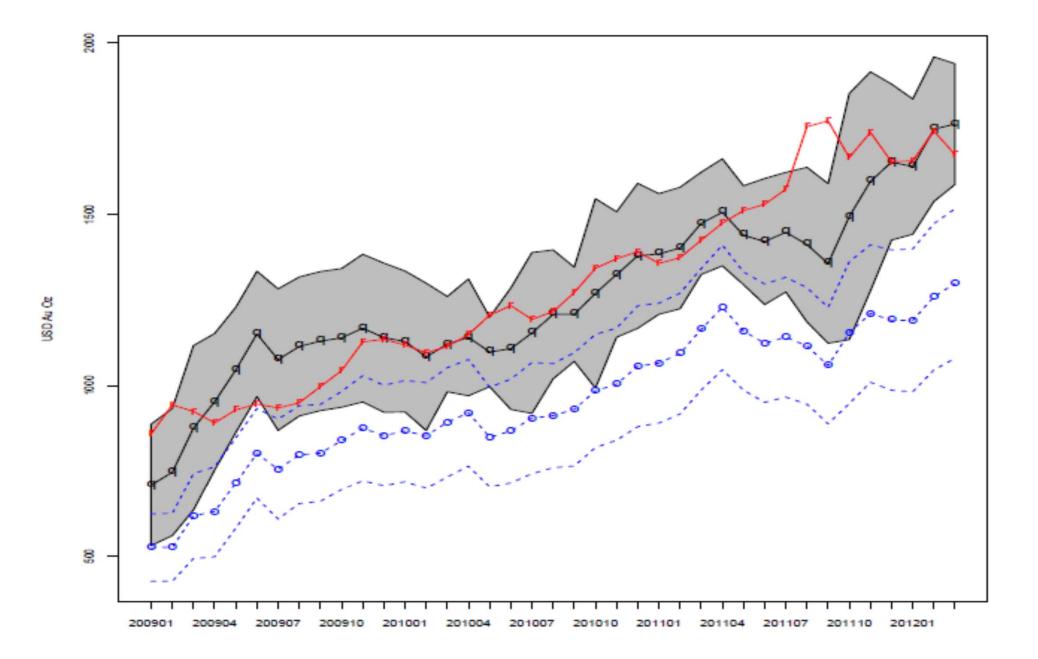


Inflation hedge? Not recently...

Inflation vs. Gold Price in different periods



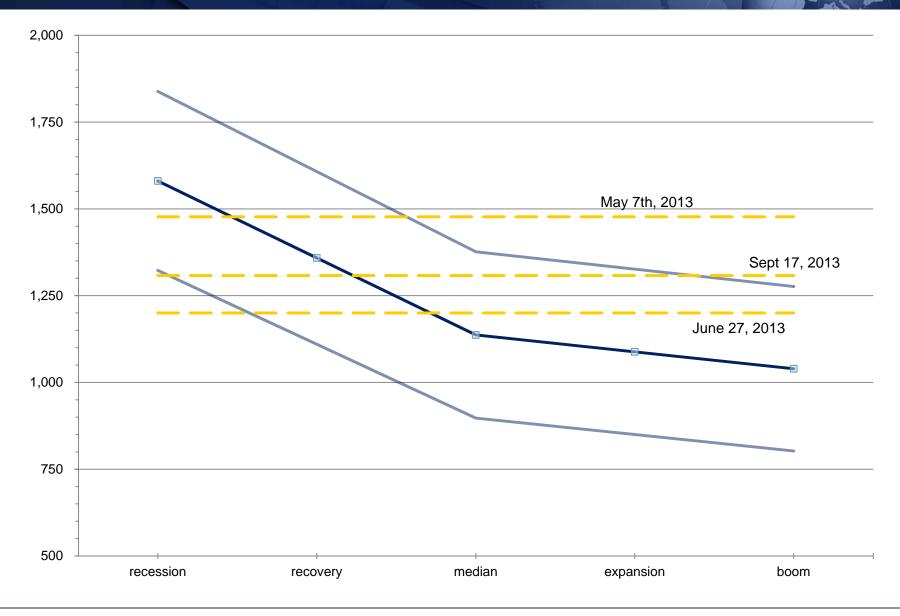




Out of Sample - Economic Scenarios

Economic Scenario	Real Inflation	Expected Inflation	Unemployment	Nominal GDP	T-bill yield	USD Index	WTI
Recession	3.32	1.54	8.91	3.9	0.04	71.16	98.06
Recovery	2.99	2.02	7.16	4.31	1.77	78.76	90.57
Median	2.65	2.49	5.4	4.71	3.49	86.36	83.08
Expansion	2.69	2.55	5.23	4.98	3.6	88.66	80.98
Boom	2.72	2.61	5.05	5.24	3.7	90.96	78.87

Out of Sample Economic Indicator



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